

## Introduction

- Infrastructure systems depend on each other to function properly and they have evolved into a network of networks.
- Interdependencies between these systems allow disruptive events to propagate across networks.
- Advances have been made in studying relatively simple, spatially constrained systems, and improved techniques are required to understand the role of interdependencies and the risks associated with them.
- This research studies interdependent networks featuring a range of complex coupling modes, and investigates the influence of these interdependencies on the behaviour and performance of interconnected systems.

## Method

A network modelling framework for exploring cascading failure of interdependent systems has been developed.

### Interdependent Network Model

- Coupling two or more networks, which can be spatial or aspatial.
- Various networks topologies, *e.g.* grid, scale free, random, centralised, decentralised *etc.* that represent different infrastructure types.
- A range of interdependency coupling modes, *e.g.* random links, favoured according to number of existing connections, preferential according to distance, which can be configured by:
  - **Directionality:** bi-directional or uni-directional
  - **Extent:** fraction of interdependent nodes
  - **Redundancy:** number of supporting connections for each interdependent node

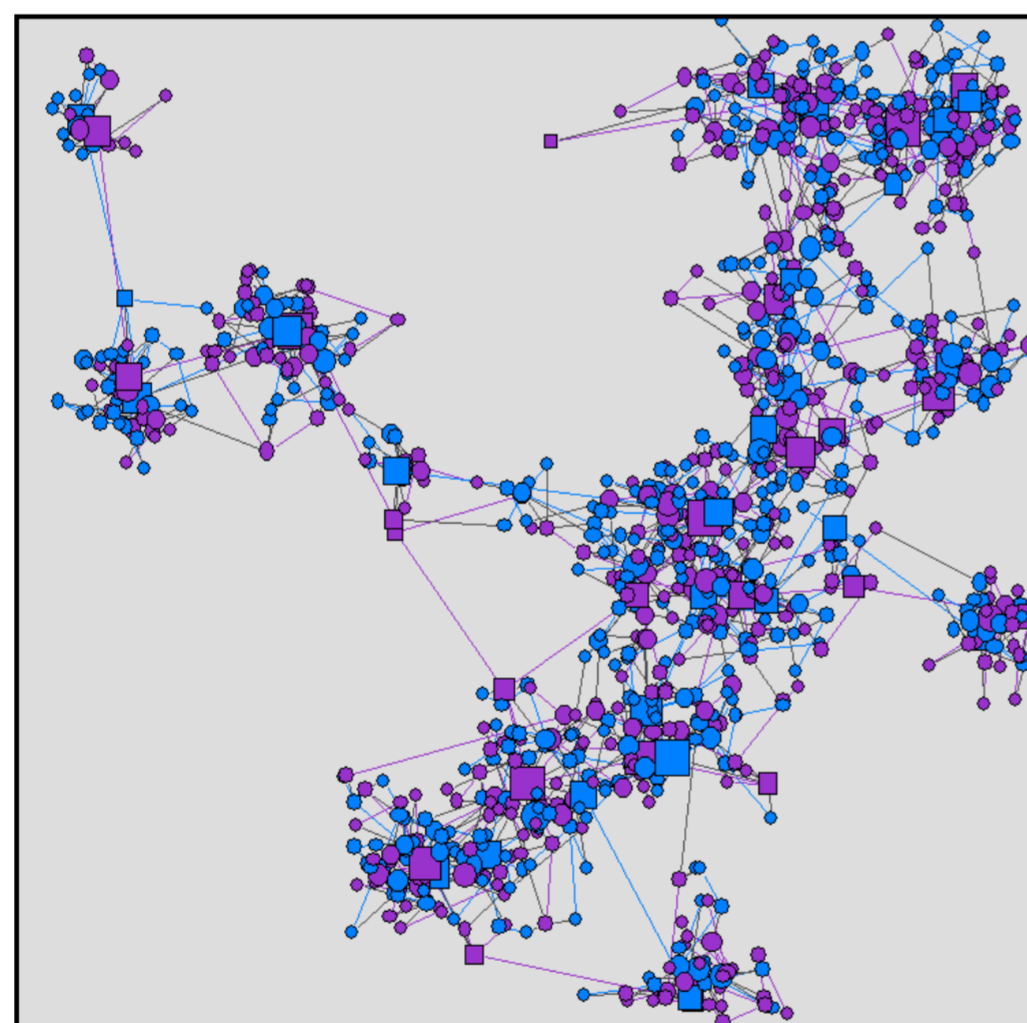


Fig. 1 An interdependent system of two networks (blue and purple). Larger nodes have more network connections. Interdependencies between each network are influenced by distance.

### Cascading Failure Model

We model an attack by disabling some proportion of the network nodes directly, which indirectly brings about a cascade of additional node failures in the system as a consequence of compromised interdependencies. An attack can be random, targeted at the most important nodes (*e.g.* largest number of connections), or spatially explicit (*e.g.* a flood, or windstorm). Node failures happen recursively and may result in system failure extending far beyond the original attack footprint, as shown in Figure 2.

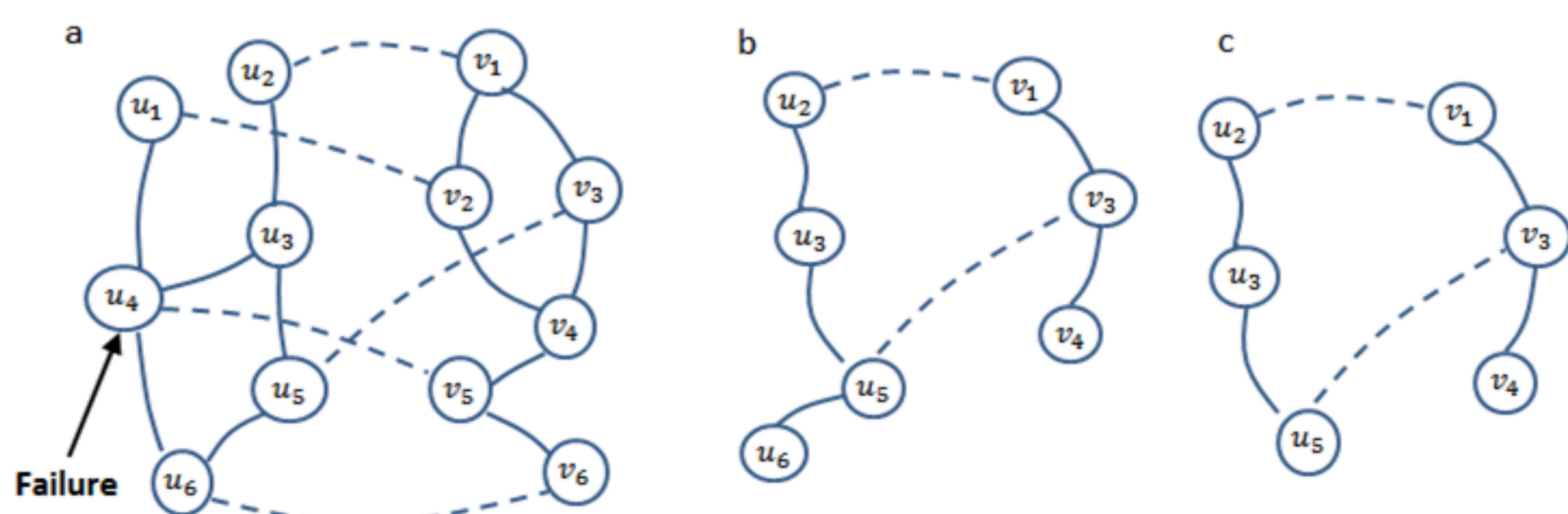


Fig. 2 An interdependent system and the cascading failure when the node  $u_4$  is attacked (a) the initial system (b) the system after the first iteration of cascading failure (c) the stabilised system.

## Results

Extensive experiments were carried out on modelled systems for a range of coupling modes. A selection of results, in each case for two coupled networks of 10,000 nodes, are reported here.

The relative size,  $P$ , of the largest connected component survived after cascading failure, is used as a measure of system performance for a given network disruption size  $q$ . The aggregate performance,  $IP$ , characterises the behaviour of an interdependent system when network disruptions of different magnitude are considered and is calculated as the integral of  $P$ .

Figure 3(a) shows how, for the system modelled here, that the introduction of interdependencies to a single infrastructure network increases its vulnerability. Figure 3(b) shows interdependencies that are uni-directional (*i.e.* if Network A node  $v$  relies upon a Network B node  $u$ ,  $u$  does not have to rely on  $v$ ) results in a more vulnerable system. This is further reinforced in Figure 3(c) which shows how increasing the fraction of bi-directional interdependencies system performance increases.

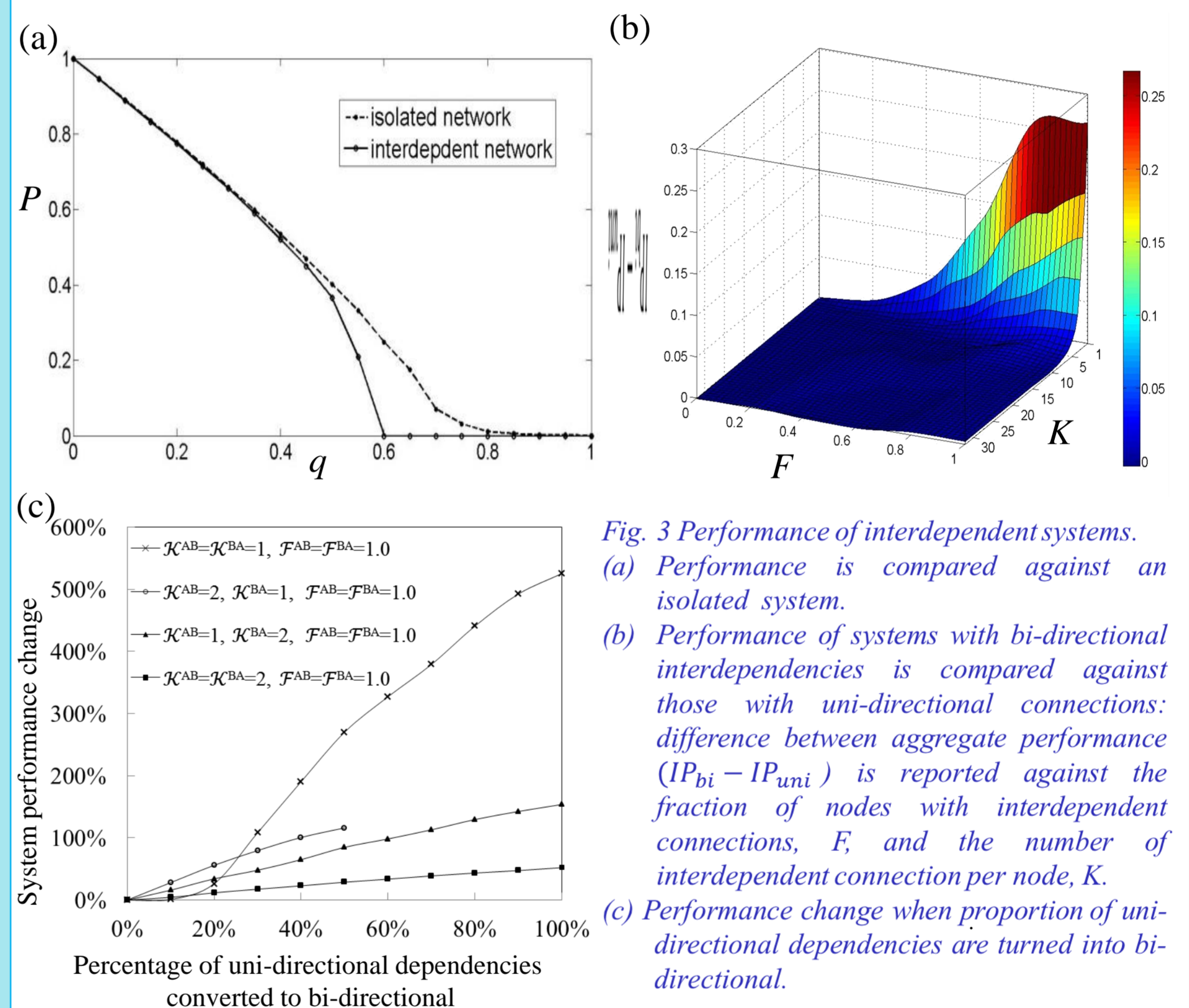


Fig. 3 Performance of interdependent systems. (a) Performance is compared against an isolated system. (b) Performance of systems with bi-directional interdependencies is compared against those with uni-directional connections: difference between aggregate performance ( $IP_{bi} - IP_{uni}$ ) is reported against the fraction of nodes with interdependent connections,  $F$ , and the number of interdependent connection per node,  $K$ . (c) Performance change when proportion of uni-directional dependencies are turned into bi-directional.

## Conclusions

- Interdependent extent, directionality and redundancy mediate the performance of interdependent infrastructure systems.
- The disruption to interdependent systems can be disproportionate to attack size when inter-network dependencies are sub-optimal.
- Networks with directed dependencies are less robust than those with undirected dependencies.
- The degree of redundancy in inter-network dependencies can have a differential effect on robustness dependent on their direction.
- The robustness of an interdependent system can be improved by optimising inter-network dependencies in a cost effective way.
- Further work is exploring the mediating influence of other network attributes, such as flow, capacity, resistance *etc.* and the development of potential transition and adaptation strategies for making interdependent networks more resilient.

### References

- Gaihua Fu, Mehdi Khoury, Richard Dawson, Seth Bullock, Cascading Failure in Networks of Networks: Impact of Redundancy and Directionality, submitted to European Physical Journal B (under review).
- Sarah Dunn, Gaihua Fu, Sean Wilkinson and Richard Dawson, Network Theory for Infrastructure Systems Modelling, submitted to Proceedings of the ICE Engineering Sustainability (under revision).